Dear Class: This is the fourth (and Week12) Portfolio Problem Set. These are momentum problems. <u>Draw lots of pictures</u>! Don't rush! The answer is surprising – and you will have learned a ton about problem solving. This is an open book and unlimited time exercise.

1) <u>CENTER OF MASS</u>

Outdoor enthusiasts Bill (mass 90 kg) and Jill (mass 60 kg) sit 3 meters apart in a symmetrical canoe of mass 120 kg. The water is calm and to one side of Bill sits a turtle on a rock in the lake watching.

- a) Find the center-of-mass position of the *people-canoe system* relative to Bill (and the turtle!).
- b) Contrary to good practice, Bill and Jill now *switch their positions* in the canoe! <u>Carefully</u> draw (don't compute!) the <u>resulting outcome</u> and answer: *Where is the center-of-mass now*?
- c) Next, **simply observe what distance** the canoe <u>must have moved</u> in the process (relative to the fixed turtle). (HINT: use symmetry!)
- d) If each person moved into the other's position in just 3 seconds, find the resulting *average velocity* with which each person moved! Who moved faster?



2) INELASTIC COLLISIONS

Bill (mass 90 kg) and Jill (mass 60 kg) form an unforgettable *acrobatic ski team*! As shown below, Bill starts from rest at the top and skis down a 200 m long straight ski slope inclined at 20°. Jill stands in the <u>middle</u> of the slope (i.e. half way down) and jumps into Bill's arms as he whizzes by.

- a) What is their speed at the bottom of the slope ?
- b) Is there an optimal position for Jill to stand so as to minimize their final speed?

