

1 **Wavelet-based optical flow**

2 **for two-component wind field estimation**

3 **from single aerosol lidar data**

4 Pierre Dérian, Christopher F. Mauzey and Shane D. Mayor\*

5 *California State University Chico, Chico, California*

6 \**Corresponding author address:* California State University Chico, 400 W. First St., Chico, CA

7 95928

8 E-mail: [sdmayor@csuchico.edu](mailto:sdmayor@csuchico.edu)

## ABSTRACT

9 A motion estimation algorithm is applied to image sequences produced by  
10 a horizontally-scanning elastic backscatter lidar. The algorithm, a wavelet-  
11 based optical flow estimator named *Typhoon*, produces dense two-component  
12 vector flow fields that correspond to the apparent motion of microscale aerosol  
13 features. To validate the efficacy of this approach for the remote measure-  
14 ment of wind fields in the lower atmosphere, an experiment was conducted  
15 in Chico, California, in 2013 and 2014. The flow fields, estimated every  
16 17 s, were compared with measurements from an independent Doppler li-  
17 dar. Time-series of wind speed and direction, statistical assessment of the  
18 10-min averages and examples of wind fields are presented. The comparison  
19 of 10-min averages at 100 m AGL reveals excellent correlations between esti-  
20 mates from the *Typhoon* algorithm and measurements from the Doppler lidar.  
21 Power spectra and spectral transfer functions are computed to characterize the  
22 filtering effects of the algorithm in the spatial domain.

## 23 1. Introduction

24 Motion estimation is a branch in the field of computer vision that develops algorithms to deter-  
25 mine the apparent movement of objects in sequences of digital images. Since the seminal paper  
26 by Horn and Schunck (1981), the applications of these numerical methods have become numer-  
27 ous; they play key roles in the success of many modern technologies including bioinformatics,  
28 video compression and machine vision. These techniques are also commonly found in experimen-  
29 tal fluid dynamics, applied for example to particle image velocimetry (PIV) (Adrian 2005). In  
30 contrast to in-situ measurements which are inherently restricted to a single point of space, motion  
31 estimation methods are non-intrusive and provide fields or volumes of velocity vectors and thus  
32 offer a broader perspective of the flow.

33 Because of the abundance of images in the atmospheric and oceanic sciences, motion estimation  
34 has been practiced since before the digital age. For example, determination of the movement of  
35 cloud features in satellite images was done prior to the work of Horn and Schunck (1981) through a  
36 block-matching approach (Leese et al. 1971). Modern applications involve for example the recov-  
37 ery of glacier velocities (Scambos et al. 1992), displacements resulting from landslides (Stumpf  
38 et al. 2013), surface water flows (Dugan et al. 2014) and breaking waves dynamics (Melville and  
39 Matusov 2002).

40 Another application, similar to PIV, involves the estimation of 2D, 2-component wind field from  
41 the apparent motion in aerosol backscatter lidar data (Schols and Eloranta 1992). Thus far the  
42 motion estimation algorithms used in that context were variations of the cross-correlation method  
43 (Mayor et al. 2012; Hamada et al. 2015). In this paper, a more recent approach that was devised  
44 specifically for application to fluid motion is investigated. This algorithm, named *Typhoon*, is  
45 a wavelet-based optical flow estimator. It was previously validated with synthetic and real PIV

46 images (Dérian 2012). Here, as a first step, the validity of this wavelet-based optical flow approach  
47 in the context of atmospheric lidar data is demonstrated.

48 The paper is organized as follows: Section 2 introduces the motion estimation framework for the  
49 wind measurement problem and the traditional cross-correlation algorithm. Section 3 presents the  
50 proposed *Typhoon* algorithm. The input aerosol backscatter lidar data is detailed in Section 4. Fi-  
51 nally, in Section 5, estimated wind fields are validated by comparisons with remote measurements  
52 from a commercial Doppler lidar. Power spectra and transfer functions are calculated to show the  
53 filtering effect of the proposed approach.

## 54 **2. Wind measurement and motion estimation**

### 55 *a. Wind measurement strategies*

56 Air motion is represented by a three-component vector and may be defined at all points in the  
57 atmosphere. The wind is generally regarded as the vector consisting of two horizontal components.  
58 Active remote wind measurement techniques may be subdivided into Doppler and non-Doppler  
59 approaches.

60 Ground-based radars and lidars typically collect data in a spherical coordinate system. Doppler  
61 radars and lidars directly measure only the radial (line-of-sight) component of air motion. For a  
62 Doppler radar or lidar to measure the wind, specific scanning strategies and assumptions about the  
63 air motion over space and time must be made. Wind profiling describes the use of a remote sensor  
64 to provide a vertical profile of horizontal wind vectors at a single location above the surface of the  
65 earth. Alternatively, two Doppler radars or lidars, separated by some horizontal distance, may be  
66 used to probe an area from different angles and obtain a two-component wind field. This approach  
67 is known as “dual-Doppler” (Stawiarski et al. 2013).

68 Non-Doppler approaches estimate wind fields from the spatial and temporal movement of fea-  
69 tures observed by the instrument. Eloranta et al. (1975) provided some of the first remote wind  
70 measurements by lidar in the lower atmosphere. Since that time, hardware and software has ad-  
71 vanced greatly and a small number of validation experiments have been conducted (Mayor et al.  
72 2012). Meanwhile, other fields, in particular experimental fluid dynamics, have developed similar  
73 approaches to retrieve motions. This concept is also known to the computer vision community,  
74 where it is associated with the wide family of *motion estimation* techniques.

75 *b. Fluid motion estimation: the vision approach*

76 The idea of using the *apparent motion of tracers* to infer the invisible underlying fluid flow is  
77 not new. It “could probably be traced far back in history to the first time a person possessing  
78 the concept of velocity watched small debris moving on the surface of a flowing stream” (Adrian  
79 2005). Many visualization methods have been developed, such as using droplets, dye, smoke or  
80 shadows for the purpose of revealing fluid flow structures and dynamics (Van Dyke 1982). This  
81 led in particular to the well-known PIV techniques, which have been used in experimental fluid  
82 dynamics for almost 30 years (Adrian 2005). Our 2D, 2-component wind measurement approach  
83 fits in the motion estimation context: the tracers are the aerosol *features*, visualized by the lidar  
84 system, and the motion estimation technique is usually the cross-correlation. This configuration  
85 is very comparable to PIV, with the important differences that the distribution of aerosols in the  
86 atmosphere (the “seeding” of the flow) cannot be controlled, and that the images are not of indi-  
87 vidual particles, but instead of a field that approximately represents particle concentration (Held  
88 et al. 2012).

89 *c. Motion estimation framework*

90 Motion estimation aims to recover the apparent displacements within a sequence of images.  
 91 The time and space variations of an observable image quantity are used to infer the underlying  
 92 motion field occurring in the image plane between two consecutive frames of the sequence. In this  
 93 work, input images are the scans provided by the lidar, the movements of the variations of aerosol  
 94 backscatter intensity are used to estimate the wind field.

95 In the following, the scan domain is noted as  $\Omega \subset \mathbb{R}^2$ . The observable backscatter intensity is  
 96 noted as  $I_n(\mathbf{x})$  at pixel  $\mathbf{x} = (x_1, x_2) \in \Omega$  and at discrete time  $t_n, n \in \mathbb{N}$ . The *apparent displacement*  
 97 between two consecutive scans  $I_n, I_{n+1}$  is a 2D vector field  $\mathbf{u}$ :

$$\mathbf{u}(\mathbf{x}, t_n) = \begin{pmatrix} u_1(\mathbf{x}, t_n) \\ u_2(\mathbf{x}, t_n) \end{pmatrix}.$$

98 This displacement is measured in pixel units and occurs over the time  $\delta t_n = t_{n+1} - t_n$  s. If the scan  
 99 has a resolution of  $\delta x$  m pixel<sup>-1</sup>, an estimation of the *instantaneous wind velocity*  $\mathbf{v}$  in m s<sup>-1</sup> is  
 100 therefore given by:

$$\mathbf{v}(\mathbf{x}, t_n) = \frac{\delta x}{\delta t_n} \mathbf{u}(\mathbf{x}, t_n). \quad (1)$$

101 As such, the motion is assumed to be stationary during the time step  $\delta t$ .

102 Velocity components  $v_1, v_2$  are the *in-plane* components, that is, they belong to the image plane.  
 103 Due to the very low value of the elevation angle of the lidar scan plane (typically  $< 6^\circ$ ), these  
 104 components coincide with the horizontal wind components (usually denoted  $u, v$  in atmospheric  
 105 sciences). The *out-of plane* component (normal to the scan plane), which remains unestimated,  
 106 thus corresponds to the vertical component  $w$ .

107 The question of the accuracy of motion estimation techniques is often raised. The answer is  
 108 complex, since it involves the *data characteristics* (spatial, temporal resolutions), the information

109 given by the *visualization method* (the image content), and the underlying *motion field* itself. In  
110 the current context, the later contributions are difficult to quantify, as they depend largely on the  
111 conditions (e.g., the presence of particulate matter, the scales and variability of the wind field).  
112 However, assuming ideal conditions and a perfect model, errors related to the resolution of data  
113 may be quantified. If displacements are measured as integers on the image grid, the systematic  
114 error is  $\pm 0.5$  pixel, which then gives  $\pm 0.5\delta_x/\delta_t$  m s<sup>-1</sup> for each motion component. In practice,  
115 various interpolation techniques allow for sub-pixel estimation, reducing this error. The error can  
116 be also lowered by using a smaller  $\delta_x$  and/or a larger  $\delta_t$ . However, for a given motion field, a  
117 smaller  $\delta_x$  results in larger apparent displacements, which can be more challenging for estima-  
118 tion algorithms. On the opposite, larger  $\delta_t$  leads to less accurate perception of the instantaneous  
119 velocity, since the assumption of stationarity of the motion field is less valid over longer periods.

120 Any motion estimation technique features two main aspects. The first one, known as the *data*  
121 *model*, describes the link between observations  $I$  (the aerosol backscatter intensity) and the under-  
122 lying unknown displacement  $\mathbf{u}$ . This model should take into account the nature of observed data  
123 and its relevant dynamics. Then, as an inverse problem, motion estimation is usually ill-posed.  
124 The second aspect is therefore the *regularization*, which is required in order to close the estima-  
125 tion problem. The regularization may also provides information where the data model fails locally.  
126 The various estimation techniques feature different data models, regularizations or implementation  
127 strategies.

#### 128 *d. The cross-correlation algorithm, concept and limitations*

129 The cross-correlation technique performs independent, local motion estimations on subregions  
130 (blocks) of the scan domain. It consists in correlating a block of the first scan  $I_n$  with a translated  
131 block of the second scan  $I_{n+1}$ ; the translation vector  $\mathbf{u}$  which induces a correlation peak is consid-

132 ered to be the displacement at the center of the block (Schols and Eloranta 1992). The estimation  
 133 problem, presented in its basic form, is written as:

$$\forall \mathbf{x} \in \Omega_C, \mathbf{u}(\mathbf{x}, t_n) = \arg \max_{\mathbf{u}} \sum_{\mathbf{y} \in B(\mathbf{x})} \frac{[I_{n+1}(\mathbf{y} + \mathbf{u}) - \mu_{n+1}(\mathbf{x} + \mathbf{u})][I_n(\mathbf{y}) - \mu_n(\mathbf{x})]}{\sigma_{n+1}^2(\mathbf{x} + \mathbf{u})\sigma_n^2(\mathbf{x})}, \quad (2)$$

134 where  $\Omega_C \subset \Omega$  is the set of block centers (and therefore the set of locations of estimated vectors),  
 135  $B(\mathbf{x})$  is the block centered on  $\mathbf{x}$ ,  $\mu_p(\mathbf{x})$  and  $\sigma_p(\mathbf{x})$  are the mean and standard deviation, respectively,  
 136 of backscatter intensity  $I_p$  over block  $B(\mathbf{x})$ . Note that in practice, this cross-correlation function  
 137 (CCF) is computed using the FFT for computational efficiency.

138 In this case, the data model is the CCF (2) itself; the regularization is implicitly given by the  
 139 size of block  $B(\mathbf{x})$  which should be large enough to contain reliable information, yet as small as  
 140 possible to resolve small scale motions. Typically, neighboring blocks overlap by 50%, so that the  
 141 estimated motion field is *sparse* (fewer motion vectors than pixels). Each vector is the result of  
 142 a single *independent* problem, which makes the CCF algorithm pleasingly parallel (Mauzey et al.  
 143 2012). This cross-correlation approach and its numerous variants have become widely used in PIV  
 144 (Adrian and Westerweel 2010); in geosciences it is often applied to satellite imagery to retrieve  
 145 for instance glacier velocities (Scambos et al. 1992), and has given good results with aerosol  
 146 backscatter lidar data, as shown in Schols and Eloranta (1992), Mayor and Eloranta (2001) and  
 147 Mayor et al. (2012).

148 However, this method as presented in (2) is not exempt from drawbacks. First, the displace-  
 149 ment within an entire block  $B(\mathbf{x})$  is explained by a single vector  $\mathbf{u}(\mathbf{x})$ , which implies that this  
 150 displacement is assumed to be uniform (constant) over the block. The larger the block, the less  
 151 likely this assumption is to be true. Yet, as overly small blocks may result in uncertainties due to  
 152 lack of information, “large” blocks are usually preferred. This leads to the second point: as dis-  
 153 placements occurring within large blocks are likely not uniform, the estimated  $\mathbf{u}(\mathbf{x})$  corresponds



154 to a power-weighted average of the apparent displacements within the corresponding block  $B(\mathbf{x})$   
155 (Hamada 2014), which results in an over-smoothed motion field. To address these issues, this  
156 study proposes to evaluate a recently developed motion estimation algorithm dedicated to fluid  
157 flows.

### 158 **3. Typhoon algorithm**

159 Early attempts with a different class of motion estimation methods, often called *optical flow*,  
160 were conducted in 2010 on the CHATS<sup>1</sup> dataset and led to promising results (Dérian et al. 2010).  
161 Since then the authors developed a new version of the algorithm based on a *wavelet* framework,  
162 named *Typhoon*. The extensive description of the algorithm is largely mathematical and details  
163 regarding the design of the data-model and the regularization can be found in Dérian et al. (2013)  
164 and Kadri Harouna et al. (2013), respectively. In the following, an overview of the method and the  
165 improvements made to achieve real-time wind estimation from aerosol backscatter lidar imagery  
166 are provided.

#### 167 *a. Optical flow, from observations to motion*

168 The proposed approach has two major differences with respect to the cross-correlation algorithm  
169 presented above. First, this wavelet-based optical flow uses a *global* formulation: all vectors  $\mathbf{u}(\mathbf{x})$   
170 of the displacement field  $\mathbf{u}$  are estimated simultaneously by solving a single problem, whereas  
171 the cross-correlation approach in (2) has as many independent problems as vectors  $\mathbf{u}(\mathbf{x})$ . Second,  
172 this method provides a *dense* estimate, that is to say one displacement vector at every point  $\mathbf{x}$   
173 of the scan domain  $\Omega$ , whereas the CCF solution is usually sparse. The estimate is obtained by

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<sup>1</sup>Canopy Horizontal Array Turbulence Study, near Dixon, CA, 2007 – see Patton et al. (2011).

174 minimizing a functional, similar to an energy, defined over the whole scan domain:

$$\mathbf{u} = \arg \min_{\mathbf{u}} \left\{ \frac{1}{2} \int_{\Omega} [f_{data}(I, \mathbf{u})]^2 d\mathbf{x} + \frac{\alpha}{2} \int_{\Omega} [f_{reg}(\mathbf{u})]^2 d\mathbf{x} \right\}. \quad (3)$$

175  $f_{data}$  is the data model that depends on observations  $I$  and unknown displacement  $\mathbf{u}$ , while the  
176 regularization  $f_{reg}$  depends on  $\mathbf{u}$  only. The parameter  $\alpha > 0$  balances the two terms and is fixed by  
177 the user.

178 The data model used in *Typhoon* is known as the displaced frame difference (DFD):

$$I_{n+1}(\mathbf{x} + \mathbf{u}(\mathbf{x}, t_n)) = I_n(\mathbf{x}). \quad (4)$$

179 It is analogous to finding the displacement field  $\mathbf{u}$  that “warps” an image into the next one. This  
180 model assumes the *consistency of backscatter intensity* along the trajectory of an aerosol feature  
181 during the time interval  $[t_n; t_{n+1}]$ , that is to say an aerosol feature will present the same intensity,  
182 the same “signature”, in both scans  $I_n, I_{n+1}$ . Therefore any phenomena inducing a significant  
183 change in intensity, such as turbulent diffusion or out-of-plane motion, can possibly lead to *false*  
184 *apparent motions*.<sup>2</sup> Such phenomena are not uncommon, but it can be reasonably assumed that  
185 the time scales at which they act are significantly larger than the inter-scan time-step  $\delta t_n$ , so that  
186 the DFD (4) remains valid. It is also important to note that from formulation (3), the data model is  
187 not *strictly* enforced. Instead, the solution achieves a balance between trying to follow the model  
188 on one hand and the regularization on the other – hence the role of the parameter  $\alpha$ , which allows  
189 the user to give more weight to one term over the other.

190 Regularization schemes usually encourage the estimate  $\mathbf{u}$  to follow some *smoothness assump-*  
191 *tion*. This work uses the most simple first-order regularization, originally introduced in Horn and  
192 Schunck (1981), which penalizes strong velocity gradients. For each displacement component  $u_i$ ,

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<sup>2</sup>False apparent motions refer here to illusory motions of aerosol features that do not correspond to the horizontal wind.

193  $i = 1, 2$ :

$$f_{reg}(u_i) = |\nabla u_i| = \sqrt{\left(\frac{\partial u_i}{\partial x_1}\right)^2 + \left(\frac{\partial u_i}{\partial x_2}\right)^2}. \quad (5)$$

194 Note that the square root is later cancelled by the square in (3). If the regularization is given much  
 195 more weight than the data model ( $\alpha \rightarrow \infty$  in (3)), the solution that minimizes (3) moves toward  
 196 a uniform motion field (with  $\nabla u_i = 0$  for  $i = 1, 2$ ). The regularizer also takes precedence over  
 197 the data model locally where the latter is inefficient, for instance within uniform regions of the  
 198 input images. Other regularizers are available in *Typhoon*, penalizing, for instance, the vorticity or  
 199 divergence of the flow, or the gradient of vorticity, divergence; some of these schemes have proven  
 200 to be very efficient with PIV and water vapor satellite images (Corpetti et al. 2002). However,  
 201 as the complexity of the regularization increases, the associated computational costs increase,  
 202 which may reduce the ability to achieve real-time estimation. Moreover, in the context of aerosol  
 203 backscatter lidar images, little to no improvement brought by the use of these advanced schemes  
 204 was found. This could be linked to the specificities of this lidar data, which will be detailed further  
 205 in Section 4.

206 The DFD model (4) and the Horn and Schunck regularizer (5) inserted into (3) complete the  
 207 motion estimation problem:

$$\mathbf{u}(t_n) = \arg \min_{\mathbf{u}} \left\{ \frac{1}{2} \int_{\Omega} [I_{n+1}(\mathbf{x} + \mathbf{u}(\mathbf{x}, t_n)) - I_n(\mathbf{x})]^2 d\mathbf{x} \right. \\ \left. + \frac{\alpha}{2} \int_{\Omega} \sum_{i=1,2} |\nabla u_i(\mathbf{x}, t_n)|^2 d\mathbf{x} \right\}. \quad (6)$$

208 A particularity of this problem is that the DFD model (4) is not linear in  $\mathbf{u}$ , so that the whole func-  
 209 tional is not quadratic. This complicates the minimization process, as the existence of a global  
 210 minimum is not guaranteed. This is another role for the regularization term: it convexifies the  
 211 functional as  $\alpha \rightarrow \infty$ . But, as large  $\alpha$  values are unmanageable, to ensure a successful mini-

212 mization it is important for the solution  $\mathbf{u}$  to lie “close” to the first guess.<sup>3</sup> This calls for the use  
213 of an incremental strategy, often known as “*multi-resolution*”: the displacement field is estimated  
214 following a coarse-to-fine process, starting with coarse structures of large amplitudes, and progres-  
215 sively refining toward smaller scales. This last point motivates the use of the *wavelet framework*.

#### 216 *b. Introduction to the wavelet framework*

217 In signal processing, the spectral space is often used to analyze or exhibit some properties of a  
218 given signal. The FFT leads to a representation in terms of sine and cosine functions of specific  
219 frequencies. Any spatial information is lost in the process: the Fourier coefficients, which form  
220 an equivalent representation of the input signal, yield no information as to *where* their associated  
221 frequency is or is not present. This is due to the fact that the sine and cosine functions, which form  
222 the basis of the spectral space, are very well localized in frequency but have an infinite support in  
223 space. Conversely, looking at the signal in the physical space does not give any information on the  
224 frequency content. The wavelet formalism offers a trade-off: the wavelet functions are localized  
225 both in space and frequency, thus they enable access to information on the *frequency content and*  
226 *the spatial location* simultaneously – at the cost of lower precision. A wavelet representation of  
227 a given signal consists of a *coarse approximation* of the signal, along with several sets of *details*  
228 containing spatially-localized information at various ranges of frequencies. Note that instead of  
229 frequency, the wavelet formalism prefers the equivalent but reciprocal notion of *scale*.

230 This multi-scale (or, multi-resolution) representation offered by the wavelet transform is the  
231 main motivation to adopt wavelet bases for displacement components  $u_1, u_2$ . It leads to a “natu-  
232 ral” coarse-to-fine strategy suitable to motion estimation (Dérian et al. 2013). Approximation and  
233 coarse detail coefficients are estimated first, then fine-scale details are successively added until

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<sup>3</sup>which is usually the null motion field,  $\mathbf{u}(\mathbf{x}) = 0 \forall \mathbf{x} \in \Omega$ .

234 the smallest scale is reached. Besides the multi-scale framework, wavelet bases also allow the  
 235 representation of arbitrary regular functions (a fluid motion field should at least be continuous).  
 236 Finally, regularization schemes presented in Section 3.a find a relatively simple yet very accurate  
 237 implementation in that context (Kadri Harouna et al. 2013). Similarly to the Fourier transform,  
 238 the wavelet transform is a linear, separable<sup>4</sup> operator, with fast algorithms (fast wavelet transform,  
 239 FWT) for computational efficiency. Wavelets are also used in many fields, from signal denois-  
 240 ing to video compression; Mallat (2008) discusses an extensive presentation of the theory and  
 241 applications.

242 Conceptually, the use of wavelet bases does not lead to significant changes to the estimation  
 243 problem (6). Each motion component  $u_i$  is expressed as the inverse transform (reconstruction) of  
 244 its corresponding wavelet coefficients  $c_i$ :

$$u_i = W_{inv}(c_i), \quad i = 1, 2,$$

245 where  $W_{inv}$  denotes the inverse wavelet transform. The set of wavelet coefficients  $\{c_1, c_2\}$  thus is  
 246 the unknown to the estimation problem.

### 247 *c. Recent improvements*

248 The original algorithm detailed in Dérian et al. (2013) would accept square images only. If  
 249 input images were rectangular, they had to be padded to turn them square, which increases the  
 250 computational burden. The current version has been modified to accept rectangular images.

251 The main improvement is the result of redesigning the code to run in “real-time”. To keep up  
 252 with real-time, the estimate of wind field  $\mathbf{v}(t_n)$  from scans  $I_n, I_{n+1}$  must be complete by the time  
 253 the next scan  $I_{n+2}$  is made available, with the inter-scan time-step  $\delta t_n$  typically on the order of  
 254 10 to 20 seconds. Since the whole motion field is estimated simultaneously, the number of vari-

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<sup>4</sup>The 2D transform is obtained by combining two 1D transform, first along rows then along columns.

255 ables is quite large: a dense estimate from  $512 \times 512$  pixel images represents about half a million  
256 unknowns. Wavelet transforms lie at the core of the estimation process. Each evaluation of the  
257 functional (6) requires two inverse FWTs (to reconstruct the displacement  $\mathbf{u}$  from its coefficients)  
258 and two forward FWTs (to compute the gradient). In order to achieve the necessary reduction in  
259 computation time, the low-level functions of the algorithm – in particular, the wavelet transforms  
260 – were rewritten in *CUDA language*, which enables it to execute on NVIDIA’s graphic processing  
261 units (GPU). GPUs designed for scientific computing rely on several thousands of small com-  
262 puting units, thus providing massive parallelization capabilities. The CUDA version of *Typhoon*  
263 running on an NVIDIA GeForce GTX Titan is 10 to 100 times faster than the original version  
264 (Mauzey et al. 2014), and is sufficient to meet the real-time requirements.

#### 265 **4. Application to aerosol backscatter data**

266 The results presented hereafter have been obtained from data collected by the Raman-shifted  
267 Eye-safe Aerosol Lidar (REAL) (Mayor and Spuler 2004; Spuler and Mayor 2005; Mayor et al.  
268 2007; Spuler and Mayor 2005) in 2013 and 2014 in Chico, California. This section describes the  
269 input data as well as the preprocessing steps.

##### 270 *a. Data preprocessing*

271 Before motion estimation takes place, the raw signal delivered by the REAL must be prepro-  
272 cessed. Lidar data is sampled on a polar grid, with the lidar at the origin. Each scan is composed  
273 of *shots*, with a shot being a 1D array of backscatter samples, uniformly spaced along the range  $r$   
274 every 1.5 m, collected at a given angular position  $\theta$  from a *single laser pulse*.

275 The raw backscatter intensity  $I_{raw}(r, \theta)$ , with the range  $r$  and the azimuth angle  $\theta$ , corresponds  
 276 to the actual backscatter signal  $\beta(r, \theta)$  and an additive noise  $\varepsilon(r, \theta)$ .

$$I_{raw}(r, \theta) = \beta(r, \theta) + \varepsilon(r, \theta).$$

277 The noise  $\varepsilon$  combines contributions from the atmosphere and the instrument and can be modeled  
 278 by a random variable which follows a normal distribution of mean  $\mu_\theta$  and standard deviation  $\sigma_\theta$ .  
 279 Values of  $\mu_\theta$ ,  $\sigma_\theta$  change slightly from one shot to another, hence their dependency in  $\theta$ ; they can  
 280 be estimated for each shot from background data. As explained in Mayor et al. (2012), first the  
 281 noise mean is subtracted:

$$I_0(r, \theta) = I_{raw}(r, \theta) - \mu_\theta = \beta(r, \theta) + \varepsilon_0(r, \theta),$$

282 with  $\varepsilon_0(r, \theta) = \varepsilon(r, \theta) - \mu_\theta$  the now centered random noise. The raw signal-to-noise ratio (SNR)  
 283 is computed at that point:

$$SNR_{raw}(r, \theta) = \frac{I_0(r, \theta)}{\sigma_\theta}. \quad (7)$$

284 Shots are then multiplied by the square of the range to compensate for the one-over-range-squared  
 285 decay of the backscatter  $\beta$ :

$$I_{r^2}(r, \theta) = r^2 I_0(r, \theta) = r^2 \beta(r, \theta) + r^2 \varepsilon_0(\theta).$$

286 Note that the noise amplitude now increases as the square of the range. For optimal results, it is  
 287 then essential to discard irrelevant noisy data, which is discussed further.

288 After conversion to decibels, shots are filtered in the range dimension. The low-pass median  
 289 filter of length 7 points (10.5 m) removes high-intensity spikes typically caused by hard-targets  
 290 such as birds and insects, while the high-pass median filter of length 333 points (500 m) removes  
 291 the very large structures to reveal local fluctuations. Figure 1 presents an example of preprocessed  
 292 backscatter data (panel a), along with the corresponding raw SNR (7) (panel b).

293 *b. Detecting coherent features*

294 Two different aspects complicate the motion estimation process. First, due to the nature of  
 295 backscatter data, the raw SNR (7) decays as one-over-range-squared. Typically, for the REAL  
 296 operating in Chico, CA, the SNR resulting from a single laser pulse drops below 5 at  $r = 3$  km.  
 297 Such high levels of noise in the far range are challenging for optical flow. Second, for the purpose  
 298 of motion estimation, a good SNR in the near range does not necessarily imply useful information.  
 299 For instance, coherent features can be absent from a region of the scan, yielding much uncertainties  
 300 as to the underlying wind field in that region.

301 In order to maximize the quality of the results, the scan areas presenting no coherent aerosol fea-  
 302 tures are discarded. Because of the regularization schemes provided by optical flow (Section 3.a),  
 303 wind vectors estimated over noisy areas *could* be relevant. However judging so proves to be diffi-  
 304 cult, as often even a basic visual confirmation is impossible in noisy regions. Hence, it is safer to  
 305 simply discard the noisy image data before motion estimation.

306 To detect the presence of coherent aerosol features, the *image SNR* is used. It is defined as the  
 307 ratio of the *local* standard deviation of coherent signal  $\sigma_\beta(r, \theta)$  to the *local* standard deviation of  
 308 noise  $\sigma_\epsilon$ :

$$SNR_{img}(r, \theta) = \frac{\sigma_\beta(r, \theta)}{\sigma_\epsilon(r, \theta)}. \quad (8)$$

309 This ratio is estimated from the autocovariance function of preprocessed data  $I(r, \theta)$ . For every  
 310 point  $(r, \theta)$ , the autocovariance  $C_l$  is computed along the range from data in  $[r - l/2; r + l/2]$ .  
 311 Then, the local variance of coherent signal is given by the average of coefficients at lag 1 and -1:

$$(\sigma_\beta)^2 = 0.5(C_l(-1) + C_l(1)),$$

312 while the local variance of noise is obtained from the 0-lag coefficient and  $\sigma_\beta$ :

$$(\sigma_\epsilon)^2 = C_l(0) - (\sigma_\beta)^2.$$



313 An example of image SNR is shown in Fig. 1 panel c. A 256-point window was used to compute  
314 the autocovariance, corresponding to  $l = 384$  m.

315 From the image SNR, a valid data domain is computed for each scan. It is assumed that the best  
316 data is in the near range, therefore the valid domain is simply defined by a far-range boundary. For  
317 each shot (azimuth  $\theta$ ), this far-range boundary is given by the smallest range  $R(\theta)$  above which  
318 the image SNR remains below a threshold  $\tau$  fixed by the user:

$$\forall \theta, R(\theta) = \min_R \{ R : \forall r > R, SNR_{img}(r, \theta) < \tau \} . \quad (9)$$

319 Finally, a low-pass median filter of width 25 points and a Gaussian filter of parameter  $\sigma = 2$   
320 points are applied to the set of  $R(\theta)$ , to exclude small isolated features and smooth the boundary.  
321 An example of mask representing the valid data domain is shown in Fig. 1 panel d, using  $\tau = 3$ .

### 322 c. Correction of image distortions

323 A lidar scan does not correspond to an instantaneous view of the aerosol distribution. The shots  
324 which the scan is composed of are acquired sequentially. In the event of high wind speeds, this  
325 leads to apparent distortions of the aerosol features in the lidar images, which in turn causes the  
326 estimation motion to be biased. This issue was first noted by Sasano et al. (1982) who proposed an  
327 iterative correction method. Assuming that the aerosol features are transported *without deforma-*  
328 *tion* by a uniform wind vector, scans can be warped to reconstruct an approximated instantaneous  
329 view of the aerosols, thus improving the accuracy of motion estimation. In this study, implemen-  
330 tation proceeds as follows for a given scan pair:

- 331 i. Estimate the displacement field  $\mathbf{u}$  from the pair of scans with the *Typhoon* algorithm.
- 332 ii. Convert to velocity field  $\mathbf{v}$  using (1).

- 333 iii. Correct both scans for distortions using wind field  $\mathbf{v}$ , following Sasano et al. (1982). The time  
334 of the beam at the center of the scan is used as the reference time.
- 335 iv. Repeat i–iii until mean wind speed  $|\bar{\mathbf{v}}|$  changes by either less than 1%, or less than  $0.25\delta x/\delta t$ .  
336 Typically, it requires 2-3 iterations.

337 The correction step (iii) is carried on the polar grid data. After correction, backscatter data is no  
338 longer known on a regular polar grid, but instead is at scattered locations.

#### 339 *d. Cartesian gridding*

340 After preprocessing, masking and correction for distortions, the backscatter data is interpolated  
341 on a Cartesian grid of spacing  $\delta x = 8$  m. It is possible to perform the motion estimation directly  
342 on the original polar grid, however, as mentioned above, the correction step destroys the regularity  
343 of the mesh. Fast interpolation on large sets of scattered data can be challenging, considering  
344 real-time requirements. In this work, a CUDA implementation of nearest-neighbor interpolation  
345 was used.

## 346 **5. Validation**

347 A field experiment was conducted in Chico, CA, from mid-September 2013 to mid-January  
348 2014, to validate the wind fields recovered by *Typhoon*. A Doppler lidar (DL) was deployed to  
349 provide independent wind measurements. It is a pulsed, heterodyne detection Doppler lidar com-  
350 mercialized by HALO Photonics under the name Streamline (Pearson et al. 2009). The DL was  
351 previously certified against cup anemometer measurements (G. Pearson 2014, personal commu-  
352 nication). DL data was filtered following the manufacturer’s indications, keeping only points for  
353 which the minimum SNR intensity  $> 1.01$ .

354 Since it is not possible to retrieve a 2D 2-component wind field using a single DL, two different  
355 configurations were investigated.

356 • *Temporal validation.* The DL was located at 1500 m range,  $15^\circ$  azimuth from the REAL  
357 and operated in vertical profiling mode. Data from this configuration enable comparisons of  
358 time-series of *2-component* wind velocities *at the DL location*. This phase of the experiment  
359 was conducted during September and October 2013.

360 • *Spatial validation.* The DL was located on the roof of the REAL container and operated  
361 in fixed-beam mode, staring at the center of the sector scan area swept by the REAL. This  
362 configuration enables one to compare *radial wind* velocity components *along the DL line-of-*  
363 *sight*. Data for this second phase of the experiment were collected in December 2013 and  
364 January 2014.

365 The main parameters used by both systems during these two experiments are summarized in Ta-  
366 ble 1.

#### 367 *a. Temporal validation*

368 In this experiment, the REAL scans between  $-15^\circ$  and  $45^\circ$  azimuth, with a  $4^\circ$  elevation, every  
369 17 s. This places the scan at 100 m AGL at the range of the DL. The DL operates in vertical  
370 profiling mode (VAD scan), providing a profile of 2-component horizontal wind vector about  
371 every 15 s.

372 A typical example of aerosol motion estimation is presented in Fig. 2. It features a close-up of  
373 two motion fields estimated from three successive position plan indicator (PPI) scans. The flow is  
374 relatively uniform, and can be visually identified due to a large aerosol feature that moves toward

375 the southeast. The DL wind vectors at 100 m AGL are displayed for comparison and show a good  
376 agreement with the *Typhoon* estimates.

377 In this paper, an effort is made to establish the potential of the *Typhoon* algorithm when applied  
378 to aerosol backscatter lidar data. However, quality of the data depends upon the performance of  
379 the instrument and the state of the atmosphere. Therefore, we selected the days presenting the  
380 best potential for this validation among data collected in Chico, CA from mid-September to mid-  
381 November 2013, with the expectation that future advances in hardware will lead to increases in  
382 data quality and availability. First, due to the local typical conditions in Chico, aerosol backscatter  
383 imagery is much better for this application during the daytime than during nighttime. There-  
384 fore, this study was restricted to daytime only. Second, the percentage of valid backscatter data  
385 (Sec. 4.b), during daytime, in a 50 m radius around the DL were computed. These values are  
386 plotted against the mean wind speed measured by the DL the same day in Fig. 3. With a suffi-  
387 cient spatial distribution of aerosol features, dense 2-component wind fields can be delivered up to  
388 several km in range. Figure 4 shows an example of such wind field on a day with high speed and  
389 uniform direction, with vectors available out to 4 km range. The low-SNR area in the far-range  
390 were dynamically excluded. Figure 5 presents a view of a  $\approx 200$  m vortex, illustrating the ability  
391 of *Typhoon* to extract coherent structures at intermediate scales.

392 Three specific cases are described below: light, moderate and strong wind conditions. These  
393 days are represented by solid diamonds in Fig. 3. For each case, time-series of instantaneous and  
394 10-min averaged wind measurements are presented. 10-min averages are the reference measures  
395 for instrument validation in the wind power industry (Bailey 2012). Then, statistics on 10-min  
396 averages for the 15 days having more than 85% valid data are presented.

397 The VAD scan strategy used by the DL assumes that the wind is uniform throughout the swept  
398 area (Mann et al. 2009, 2010; Sathe et al. 2011; Sathe and Mann 2012); in this case this region is a

399 disc of about 100 m radius, represented by a turquoise circle in Figs. 4 and 5. In order to compare  
400 results of the study to the DL measures, instantaneous *Typhoon* estimates are averaged in space  
401 over a similar sized area centered on the DL location.

402 Occasionally, the estimation may fail and result in obvious outliers. Those outliers can be de-  
403 tected and removed under the assumption of temporal coherence of the wind field. The *normalized*  
404 *median test*, commonly used in PIV (Adrian and Westerweel 2010), was implemented. Similar  
405 concepts are used with radar wind profilers (Weber et al. 1993). Within each 10-min window, the  
406 median wind vector  $\mathbf{v}_m$  is computed, as well as the residuals  $r(\mathbf{v}) = |\mathbf{v}_m - \mathbf{v}|$  for each vector  $\mathbf{v}$  of  
407 the window. Vectors for which the residual  $r(\mathbf{v})$  is twice larger than the median of residuals  $r_m$  are  
408 discarded.

#### 409 1) LIGHT WIND CASE

410 Figure 6 shows wind speed and direction measured by the DL at 100 m AGL and estimated  
411 by *Typhoon* for a 12-hour period starting on October 23 at 15:00 UTC. It is a light wind episode  
412 with speeds remaining below  $3 \text{ m s}^{-1}$  and variable direction. Estimates are missing over a pe-  
413 riod approximatively covering 15:00 to 17:00 UTC. This is due to the coherent feature detection  
414 presented in Sec. 4.b: no significant features were present in the region of interest at that time,  
415 therefore no motion estimates are available. Then, between 17:00 and 18:00 UTC, *Typhoon* speed  
416 and direction estimates are in systematic error. Visual inspection of the aerosol imagery reveals  
417 the mixed layer growing with the entrainment zone passing through the altitude of the intercom-  
418 parison. It appears that the plumes and wind shear in the entrainment zone result in false apparent  
419 motions that bias the motion estimations. Later, two reversals of wind direction occurred at 22:30  
420 and 23:30 UTC that correspond to the passage of a vortex of diameter  $\approx 200 \text{ m}$  over the region  
421 of interest (see also Fig. 5 for a spatial visualization). This microscale circulation resembles those

422 that have resulted from large eddy simulation of convective boundary layers (Schmidt and Schu-  
423 mann 1989; Kanak 2005; Sullivan and Patton 2011). Correlation coefficients  $R^2$  for the 10-min  
424 averaged wind components are 0.951 and 0.600 for  $u$  and  $v$ , respectively. Excluding the 17:00 –  
425 18:00 UTC period with false apparent motions,  $R^2$  values increase to 0.966 and 0.866.

## 426 2) MODERATE WIND CASE

427 Figure 7 shows wind speed and direction measured by the DL at 100 m AGL and estimated  
428 by *Typhoon* for a 12-hour period starting on September 17 at 15:00 UTC. This wind episode fea-  
429 tures speeds ranging 0 to 10 m s<sup>-1</sup> and direction mostly stationary except for a 2-hour fluctuating  
430 episode (corresponding to the lowest wind speeds). Wind speed is underestimated at two occa-  
431 sions, both corresponding to rapid and large changes in direction around 22:30 and 23:00 UTC.  
432 Otherwise, both series of data are in very good agreement. This is confirmed by the 10-min aver-  
433 aged wind components: correlation coefficients  $R^2$  are 0.979 and 0.991 for  $u$  and  $v$ , respectively.

## 434 3) STRONG WIND CASE

435 Figure 8 shows wind speed and direction measured by the DL at 100 m AGL and estimated  
436 by *Typhoon* for a 12-hour period starting on October 9 at 15:00 UTC. It is a strong wind episode  
437 with speeds up to 16 m s<sup>-1</sup> and very consistent flow from the northwest direction. Both time-  
438 series are again in very good agreement. Correlation coefficients  $R^2$  for the 10-min averaged wind  
439 components are 0.984 and 0.929 for  $u$  and  $v$ , respectively.

## 440 4) OVERALL CONSIDERATIONS

441 Scatter plots of 10-min averaged wind components measured during the daytime<sup>5</sup> for the 15  
442 “best” days (Fig. 3) are presented in Fig. 9. They show an overall excellent agreement of *Typhoon*

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<sup>5</sup>“Daytime” is arbitrarily considered to be 15:00 – 01:00 UTC (10 hours).

443 estimates with DL measurements at 100 m AGL: correlation coefficients  $R^2$  are 0.995 and 0.997  
444 for  $u$  and  $v$ , respectively. Detailed statistics on  $u$  and  $v$  are available in Tables 2 and 3. In terms of  
445 wind speed, a linear regression gives a slope of 1.000 with an offset of  $-0.10 \text{ m s}^{-1}$ ,  $R^2$  coefficient is  
446 0.991. Regarding the wind direction, the offset is  $1.1^\circ$  and  $R^2$  coefficient is 0.944.<sup>6</sup> This  $\approx 1^\circ$  offset  
447 observed for the direction corresponds to the precision at which the DL was oriented during its  
448 deployment. The standard deviations (std) of observed differences is  $0.29 \text{ m s}^{-1}$  on both on  $u$  and  
449  $v$  components. This is slightly higher than the expected systematic error of  $0.5\delta_x/\delta_t \approx 0.24 \text{ m s}^{-1}$   
450 which assumes perfect data and model (Sec. 2.c). The few remaining outliers mostly correspond  
451 to false apparent motions, typically occurring at the beginning and end of the day as the boundary  
452 layer depth evolves.

453 From the time-series shown in Figs. 6, 7 and 8, it appears the variability of the wind speed  
454 obtained by *Typhoon* is less than that measured by the Doppler. Figure 10 is a scatter plot of  
455 turbulent kinetic energy (TKE) as measured by the Doppler and *Typhoon* over 10-min intervals.  
456 A linear regression suggests that the TKE from *Typhoon* is about 50% smaller than the Doppler's.  
457 This could be linked to the fact that *Typhoon* measures apparent displacements, which are later  
458 converted to velocities (Sec. 2.c). Small-scales velocity structures, either in time or space, are  
459 less accurately perceived. Using a faster scan rate is likely to improve the results. Nevertheless,  
460 *Typhoon* performs better than the cross-correlation technique: the optimized algorithm presented  
461 in Hamada et al. (2015) recovers 39% of the TKE on the same dataset.

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<sup>6</sup>When dealing with circular data such as angles, the slope for the linear regression should be fixed to 1. The offset and  $R^2$  only are computed, see e.g. Fisher (1995).

462 *b. Spatial validation*

463 During this phase of the experiment, the DL was colocated with the REAL. The REAL swept  
464 between  $15^\circ$  and  $75^\circ$  azimuth at  $2^\circ$  elevation every 17 s. The DL held its beam fixed at  $45^\circ$  azimuth  
465 and  $2^\circ$  elevation, measuring the radial velocity component as a function of range and time. DL  
466 measurements were integrated over one second, with a range gate of 48 m. The temporal resolution  
467 of DL measurements is therefore much finer than that of the REAL flow fields, and conversely for  
468 the spatial resolution (see Table 1).

469 Instead of holding the DL beam fixed, a PPI sweeping strategy identical to the REAL's could  
470 have been used, thus allowing the comparison of radial components over the whole scan domain.  
471 However, two arguments support the choice of a fixed beam:

- 472 • With a moving beam set-up, the integration time for DL measurements was reduced to less  
473 than 0.1 s. This would cause the SNR to decrease very rapidly. Typically in Chico the  
474 maximum range with useful data would be on the order of 1500 m, significantly below that  
475 of the REAL's.
- 476 • The radial velocity fields collected by the DL would suffer from the same distortions as the  
477 backscatter data (Section 4.c), so correcting these distortions would be challenging.

478 The data used for the spatial validation were recorded in December 2013 and January 2014. In  
479 Chico, CA, the days are shorter and the air is cleaner during this season than in the autumn when  
480 time-series data were collected. Both the DL and the REAL are affected. Data are of lower quality  
481 than shown for the temporal validation. The availability of 10-min averages falls below 50% after  
482 3 km for both instruments and at 5 km it is below 5%. Therefore, the analysis is restricted to the  
483 first 3 km. Furthermore, it should be noted that the prevailing wind direction during this time over  
484 Chico, CA is northwesterly. At  $45^\circ$  azimuth, the line-of-sight component corresponds mostly to



485 the *cross-stream*, turbulent wind perturbations. In these data, its magnitude remains mostly below  
486  $3 \text{ m s}^{-1}$ . Figure 12 shows a comparison of radial velocity measured by the DL and extracted from  
487 the 2-component fields obtained by *Typhoon* for a 8-hour period starting 8 January 2014 at 17:00  
488 UTC.

489 In order to compute statistics, radial velocities were averaged. First, spatial resolution are  
490 matched by averaging *Typhoon* velocities in space according to DL range gates, then 10-min time-  
491 averages are computed at every range. A scatter plot of these 10-min averages is presented in  
492 Fig. 13, along with linear regression slopes,  $R^2$  coefficient and distribution of differences. These  
493 values were obtained from 8-hour periods (17:00 to 01:00 UTC) for 8 days of December 2013 and  
494 January 2014. The  $R^2$  coefficient (panel d) decreases with the range and this is expected as both  
495 instruments are affected by the gradual reduction in SNR.  $R^2$  remains above 0.95 over the first  
496 1.5 km, then slowly decreases to about 0.8 at 3 km. The overall  $R^2$  is 0.928. While the relation  
497 between *Typhoon* and DL velocities remains linear, the slope (panel c) increases with the range,  
498 from about 0.95 at 0.5 km to 1.3 at 3 km. Velocities obtained by the cross-correlation method  
499 show a similar trend (Hamada et al. 2015). This leads to a theory that these discrepancies are due  
500 to a mismatch in the actual elevation angles of the beams during this phase of the experiment,  
501 especially considering the unbiased results of the temporal validation. At a lower elevation angle  
502 and therefore lower altitude, the DL would measure lower velocities.

### 503 *c. Spectral analysis*

504 In this section, temporal and spatial power spectra of the velocity components produced by  
505 *Typhoon* are presented, with the objective of characterizing the filtering effect of the algorithm –  
506 in particular, in the spatial domain. The velocity data analyzed were collected during the daytime

507 and within the turbulent lower atmospheric boundary layer.<sup>7</sup> Therefore, an inertial subrange in the  
508 power spectra of the actual velocity field is expected.

509 The spectra are computed in natural coordinates to account for the anisotropy of atmospheric  
510 boundary layer turbulence, The west-east and south-north wind velocity components are projected,  
511 according to the mean wind direction, as streamwise ( $u_s$ ) and cross-stream ( $v_n$ ) components, such  
512 that  $u_s$  carries the mean speed and  $v_n$  has a null mean. The mean wind vector is defined accordingly  
513 to the investigated dimension, either in time or space. The spectra are finally averaged together  
514 according to the mean wind speed, using bins of 0–4 m s<sup>-1</sup>, 4–8 m s<sup>-1</sup>, 8–12 m s<sup>-1</sup> and 12–  
515 16 m s<sup>-1</sup>, in order to exhibit their evolution with increasing wind speed and turbulent kinetic energy.  
516 The resulting power spectral densities ( $S$ ) are multiplied by frequency ( $f$ ) or wavenumber squared  
517 ( $\kappa^2$ ) so that an inertial subrange would appear as a  $-2/3$  slope and white noise would appear as  
518  $+1$  slope.

#### 519 1) TEMPORAL POWER SPECTRA

520 During the experiment, the REAL collected PPI scans every 17 s and one RHI scan every 15 min.  
521 The RHI scan resulted in an 30 s interruption of the PPI scan sequence. The scan strategy of the  
522 DL provided vertical profiles of horizontal winds every  $15 \pm 1$  s. Since the FFT requires data  
523 points at a uniform time interval, the *Typhoon* and DL wind measurements were interpolated to  
524 a 5 s time series. From the 5 s time series data, we computed power spectra over consecutive  
525 10 min intervals. The 10-min mean wind vector was used for the projection in natural coordinates  
526 and the binning of spectra, as defined above. The resulting spectra have a Nyquist frequency of  
527 0.029 Hz (34 s period) for the *Typhoon* velocities and 0.033 Hz (30 s period) for the DL. The  
528 lowest frequency is  $1.67 \times 10^{-3}$  Hz (10 min period).

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<sup>7</sup>RHI scans collected every 15 min by the REAL during the 15 days included in the analysis show that the maximum convective boundary layer height, that typically occurred in the afternoon, ranged from 300–1200 m AGL.

529 The spectra are presented in Fig. 14. Those from the Doppler lidar are consistently higher than  
530 the spectra from *Typhoon*, this is consistent with our observation that the TKE measured from  
531 Doppler velocities are larger than those from *Typhoon* (Fig. 10). The temporal spectra appear to  
532 become flatter as the mean wind speed increases. We hypothesize that this may be caused by the  
533 challenges that both *Typhoon* and the DL face under windy conditions. For the DL, increased  
534 variability of the actual wind velocity field in the VAD sample area results in more error in the  
535 horizontal wind vector estimate. The increased error appear as noise at these time scales and  
536 flatten the spectrum. For *Typhoon*, windy conditions result in larger horizontal displacements  
537 between scans and faster deformation of aerosol coherent structures.

## 538 2) SPATIAL POWER SPECTRA

539 An independent observation of the 2-component 2-D velocity field does not exist for comparison  
540 with those produced by *Typhoon*. A dual-Doppler lidar set up could have provided it, but would  
541 have doubled the cost and complexity of the project. Therefore, to investigate the integrity of the  
542 vector flow fields in space, spatial power spectra are considered.

543 A 1 km diameter circular area is considered, centered on the DL at 1.53 km range. All of the  
544 vectors within this area (from a single flow field in time) are used to compute the spatial mean wind  
545 vector, which then define a natural coordinate system. Vectors of the flow field are interpolated on  
546 a  $128 \times 128$  point grid ( $1024 \text{ m} \times 1024 \text{ m}$ ) that is centered on the DL and aligned with the natural  
547 coordinate system, and then projected as streamwise ( $u_s$ ) and cross-stream ( $v_n$ ) components. This  
548 operation was performed for each flow field independently and resulted in 30092 flows fields over  
549 15 days. At  $4^\circ$  elevation, the  $1024 \text{ m} \times 1024 \text{ m}$  area covers a range of altitudes from about 50 m  
550 to 150 m AGL. A possible impact of this is that the turbulence statistics within this sloped domain  
551 are slightly inhomogeneous. Nevertheless, for each component  $u_s$ ,  $v_n$ , the 2D power spectral

552 densities computed by FFT for each flow field are averaged together according to the mean spatial  
553 wind speed. Finally, slices of the resulting 2D power spectra were extracted along the streamwise  
554 and cross-stream directions. This results in four 1D spectra for each wind speed bin: along the  
555 streamwise and cross-stream directions, for each of the streamwise and cross-stream components.  
556 The Nyquist wavenumber is  $\kappa/2\pi = 0.0625 \text{ m}^{-1}$  (16 m wavelength), the lowest wavenumber is  
557  $9.77 \times 10^{-4} \text{ m}^{-1}$  (1204 m).

558 The spectra in the top row of Fig. 15 show the TKE increasing as expected as function of wind  
559 speed. Each spectrum has a maximum amplitude at low wavenumbers. We hypothesize that the  
560 peak corresponds to one over the Eulerian length scale, and is within the energy containing range  
561 (Kaimal and Finnigan 1994). However, the spectra are steeper than  $\kappa^{-2/3}$ . We attribute this to  
562 two factors. First is the likely absence of aerosol features at all scales and all locations in the scan  
563 area at all times. Second is the regularization used in *Typhoon* which favors a smooth motion field,  
564 especially as the estimation reaches the smallest scales.

565 A transfer function describes the ratio of two spectra and, in the present work, represents the  
566 attenuation of the actual wind field caused by the motion estimation as a function of wavenumber.  
567 A highly idealized spectrum is constructed to serve as the reference. This is done by first locating  
568 the maximum of each mean spatial spectra shown in Fig. 15. We assume that the observed power  
569 at wavenumbers smaller than the peak in the spectra are accurately captured by the algorithm and  
570 serve as a proper approximation of the power at those large scales. For scales smaller than the  
571 peak, we extrapolate by a power-law dependence through the higher wavenumbers that mimics  
572 the inertial subrange (a  $\kappa^{-2/3}$  spectrum). The transfer functions are then given by the ratio of the  
573 observed mean spectra over the idealized spectrum, and presented in the bottom row of Fig. 15.  
574 The higher the wind speed, the more energy is missing at small scales. The ratio typically drops

575 below 50% at scales of  $\approx 100$  m ( $\kappa/2\pi \approx 0.01$  m<sup>-1</sup>) for the highest wind speeds, and  $\approx 75$  m for  
576 the lowest.

## 577 **6. Broader perspectives and conclusions**

578 In a recent paper, entitled *Review of turbulence measurements using ground-based wind lidars*,  
579 Sathe and Mann (2013) conclude that “Non-coherent detection may also provide possible new  
580 ways to estimate atmospheric turbulence, but to our knowledge it does not, so far, challenge the  
581 capabilities of coherent Doppler lidars.” In this paper, we have (1) introduced a new motion  
582 estimation method; (2) made the first direct comparisons of the “non-Doppler motion estimation  
583 approach” with Doppler lidar; and (3) computed transfer functions to estimate the filtering effect  
584 of the approach. The new motion estimation method resolves finer spatial scale flow details than  
585 the traditional cross-correlation algorithm (Hamada et al. 2015). The comparisons in the time  
586 domain reveal excellent correlation in terms of 10-min averages, close for example to standards  
587 expected of commercial floating lidars (Carbon Trust 2013). However, the proposed approach still  
588 underestimates the TKE by about 50% of what is observed by Doppler lidar. It is important to  
589 keep in mind that the Doppler also provides a filtered version of the actual flow field.

590 Two horizontal components are required for wind speed and direction. The proposed approach  
591 delivers dense 2-component wind fields from a single lidar, whereas a single Doppler only pro-  
592 duces a single component. In addition to wind resource assessment, wind fields such as delivered  
593 by *Typhoon* from REAL imagery enable the visualization and investigation of meteorological phe-  
594 nomena such as vortices and fronts. They also open the possibility of studies in the Lagrangian  
595 reference frame, and the tracking of flow structures or aerosol features.

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## 599 APPENDIX A

### 600 **Mathematical Symbols**

- 601 •  $\forall$  for all;
- 602 •  $\subset$  subset of;
- 603 •  $\in$  in (belonging to);
- 604 •  $\mathbb{N}$ ,  $\mathbb{R}$  the sets of natural and real numbers, respectively.

## 605 APPENDIX B

### 606 **Parameters of *Typhoon***

607 Unless specified, results were obtained using the following parameters for *Typhoon*:

- 608 • version: cuTyphoon 1.0;
- 609 • wavelet basis: Daubechies, 10 vanishing moments;
- 610 • wavelet scales: 8 details scales considered and estimated;
- 611 • pyramid steps=1, scaling factor=50%;
- 612 • data model: DFD, smoothing kernel  $\sigma = 0.5$ ;
- 613 • regularization: Horn & Schunk,  $\alpha = 0.05$ ;
- 614 • data range:  $[-0.5, 0.5]$ , with normalization, without histogram matching.

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TABLE 1. Main parameters of DL and REAL measurements for the temporal and spatial validation experiments.

	Temporal validation		Spatial validation	
	Doppler	REAL	Doppler	REAL
scan type	VAD	PPI	STARE	PPI
azimuth (°)	–	[–15;45]	45	[15;75]
elevation (°)	–	4	2	2
range (km)	–	[0.5;5.5]	[0;5]	[0.5;5.5]
components	2	2	1	2
$\delta x$ (m)	–	8	48	8
$\delta t$ (s)	15 ±1	17	1	17

722 TABLE 2. Standard deviation of differences, linear regression variables (slope, offset), correlation coefficient  
 723  $R^2$ , number of points and recovery percentage w.r.t. DL reference for the 10-min averaged wind component  $u$   
 724 (west-east), for the temporal validation results (Sec. 5.a).

case	std dev ( $\text{m s}^{-1}$ )	slope	offset ( $\text{m s}^{-1}$ )	$R^2$	# points	% recovery
light	0.17	1.047	-0.01	0.951	61	84.7
moderate	0.29	0.974	-0.05	0.979	72	100
strong	0.33	0.938	0.32	0.984	72	100
15 days	0.29	0.989	-0.03	0.995	892	99.1

725 TABLE 3. Std dev of differences, linear regression variables (slope, offset), correlation coefficient  $R^2$ , number  
 726 of points and recovery percentage w.r.t. DL reference for the 10-min averaged wind component  $v$  (south-north),  
 727 for the temporal validation results (Sec. 5.a).

case	std dev ( $\text{m s}^{-1}$ )	slope	offset ( $\text{m s}^{-1}$ )	$R^2$	# points	% recovery
light	0.25	0.660	-0.02	0.600	61	84.7
moderate	0.23	0.999	0.00	0.991	72	100
strong	0.34	0.897	-0.72	0.929	72	100
15 days	0.29	1.001	0.03	0.997	892	99.1

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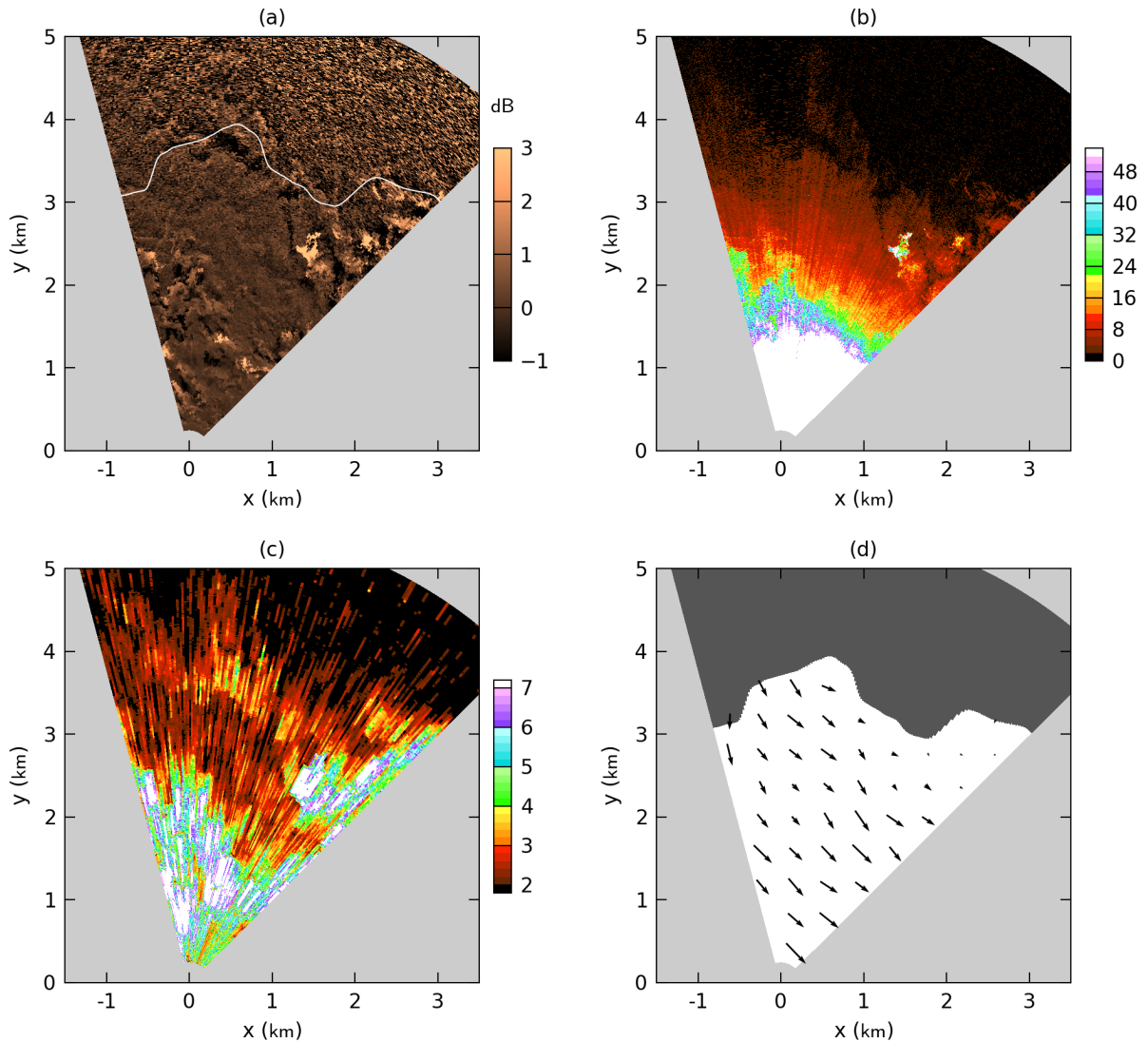
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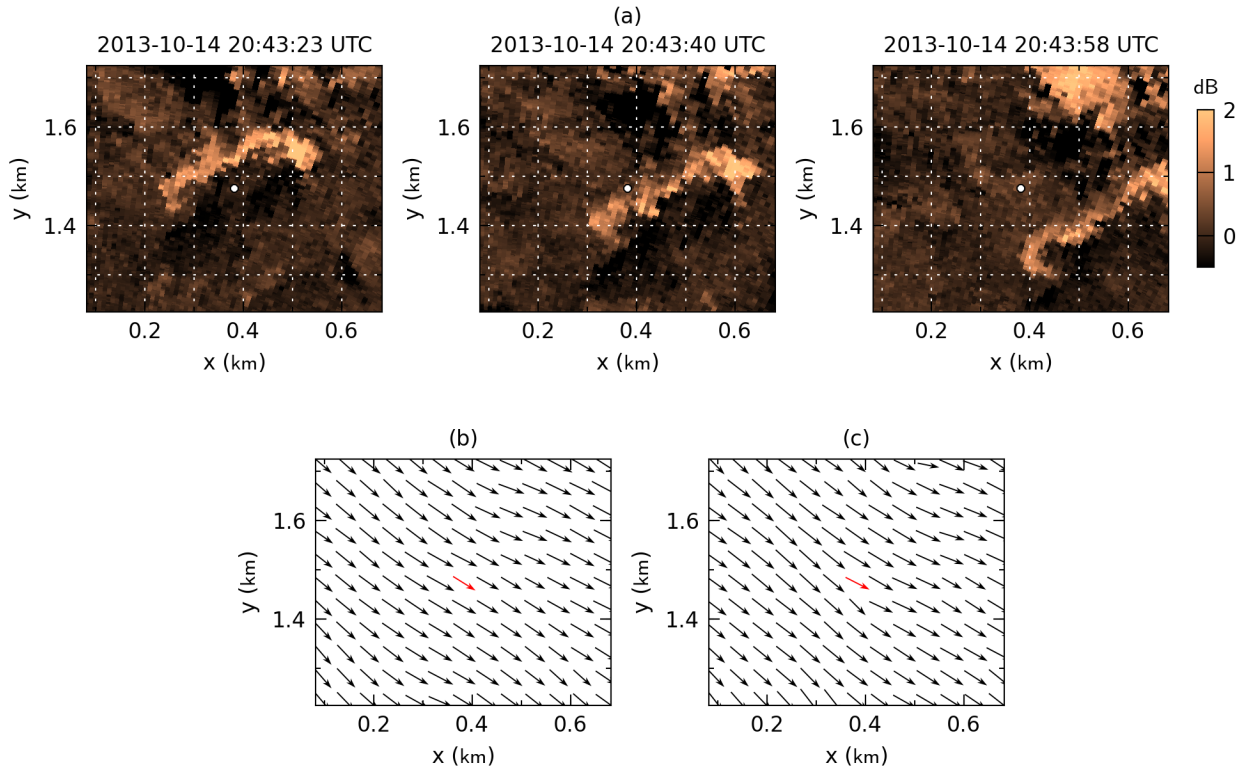
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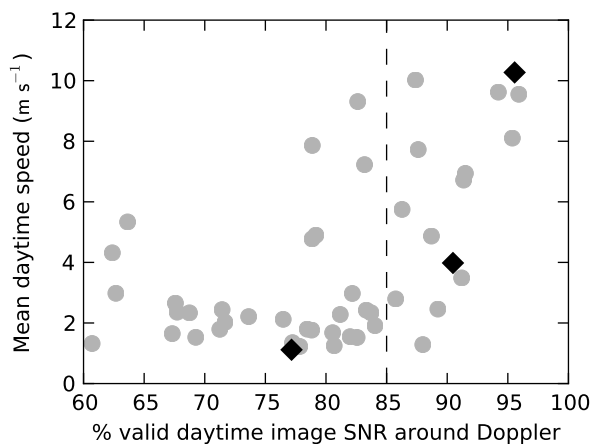
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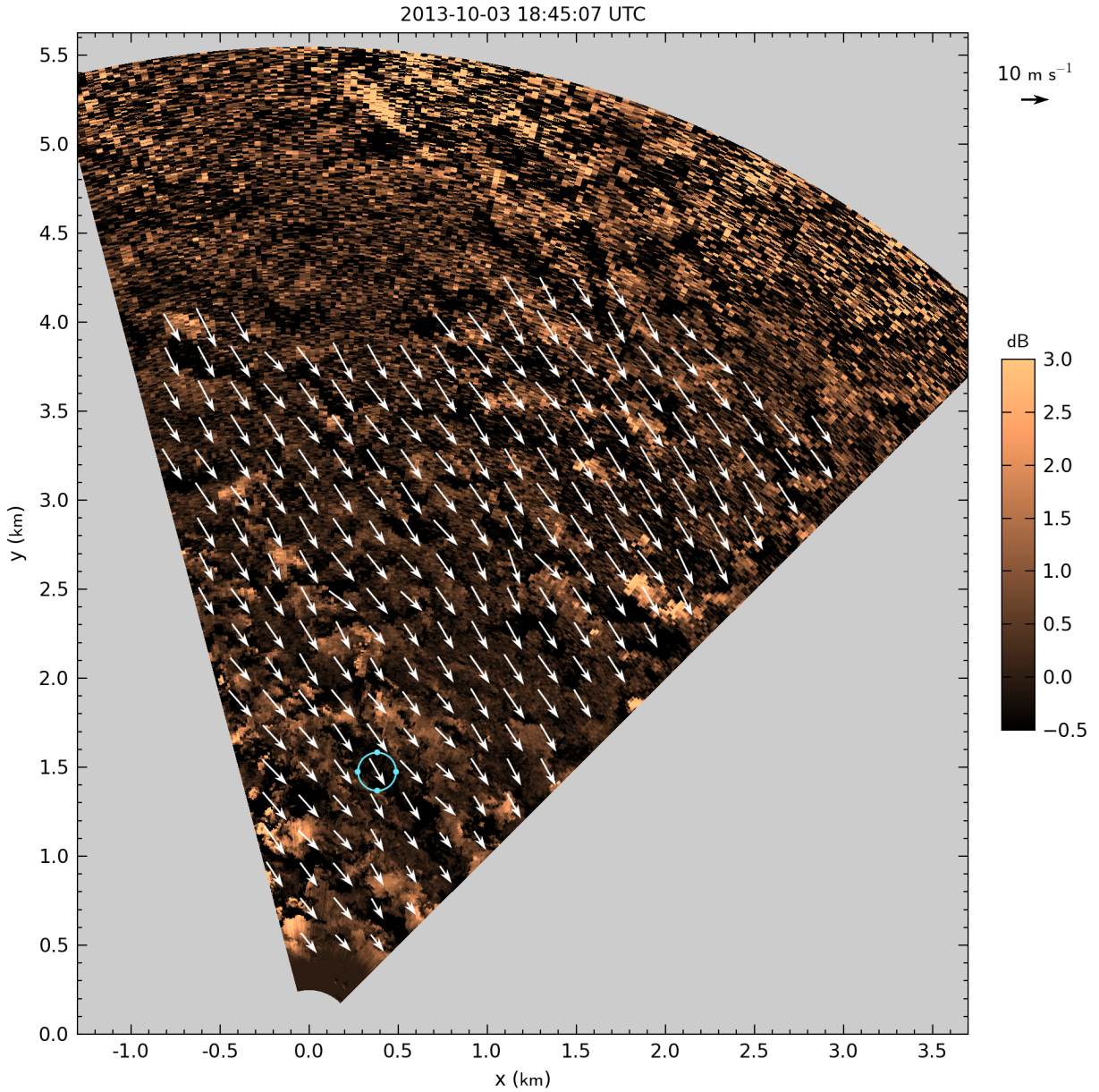
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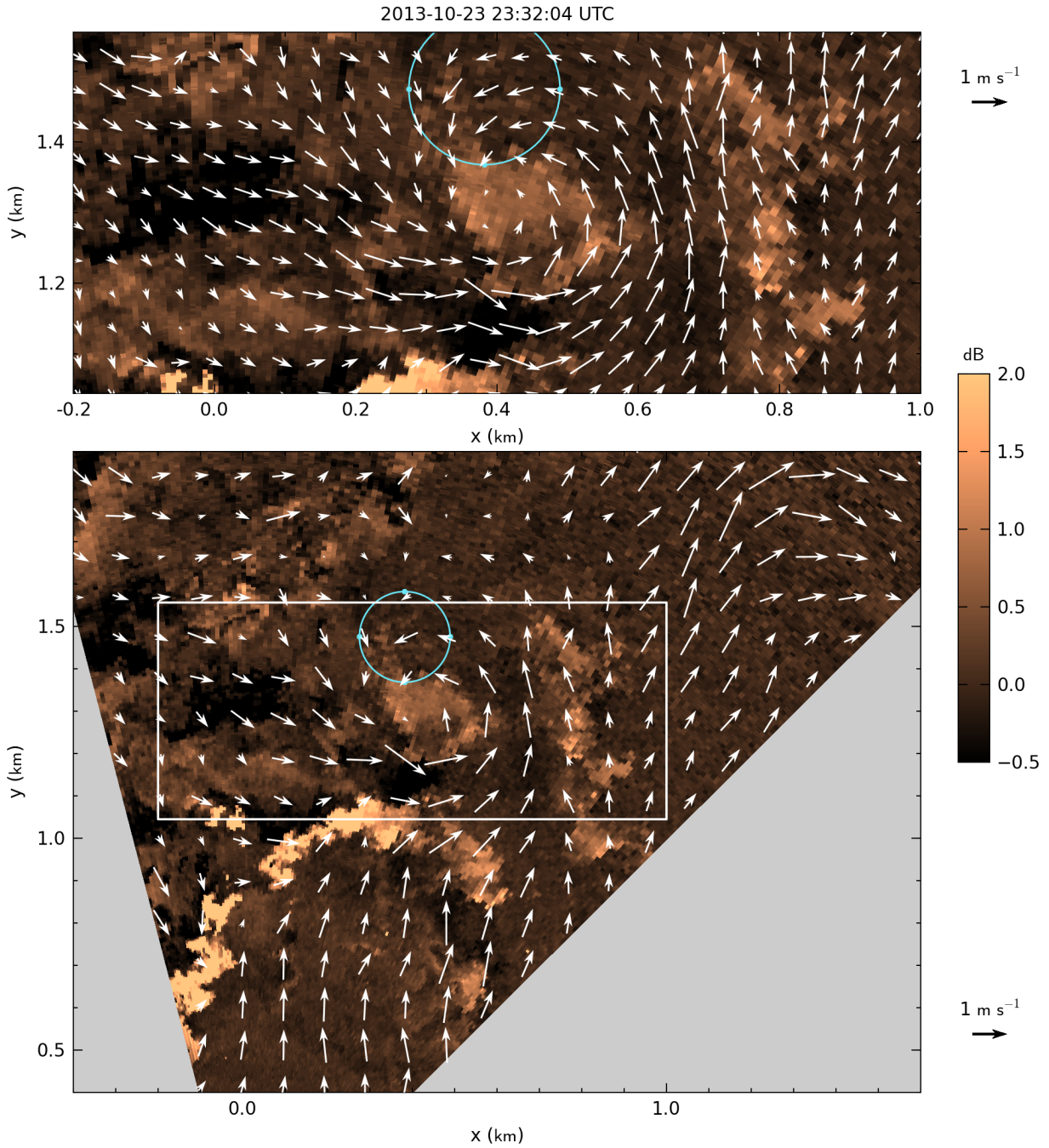


822 FIG. 3. Distribution of days in terms of valid image SNR (Sec. 4.b) in a 50 m radius around DL location  
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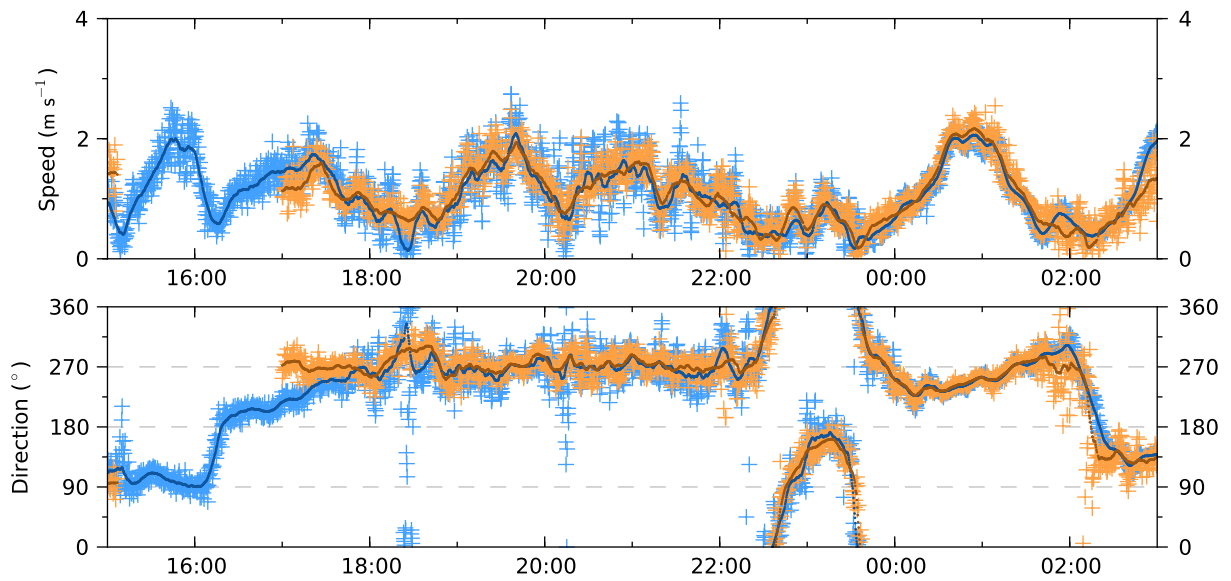


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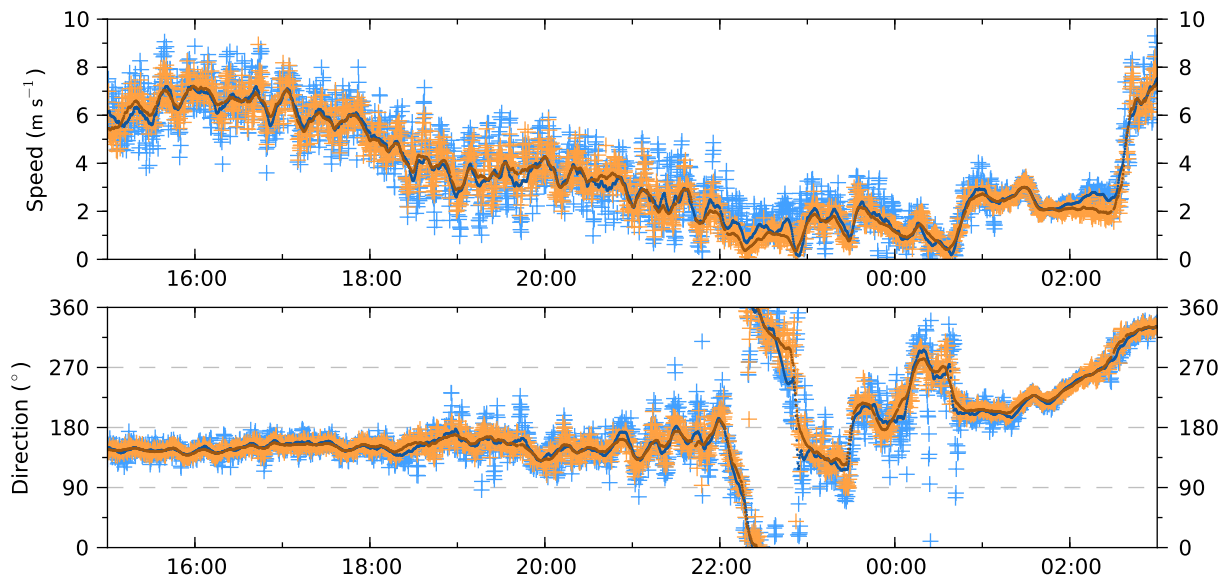




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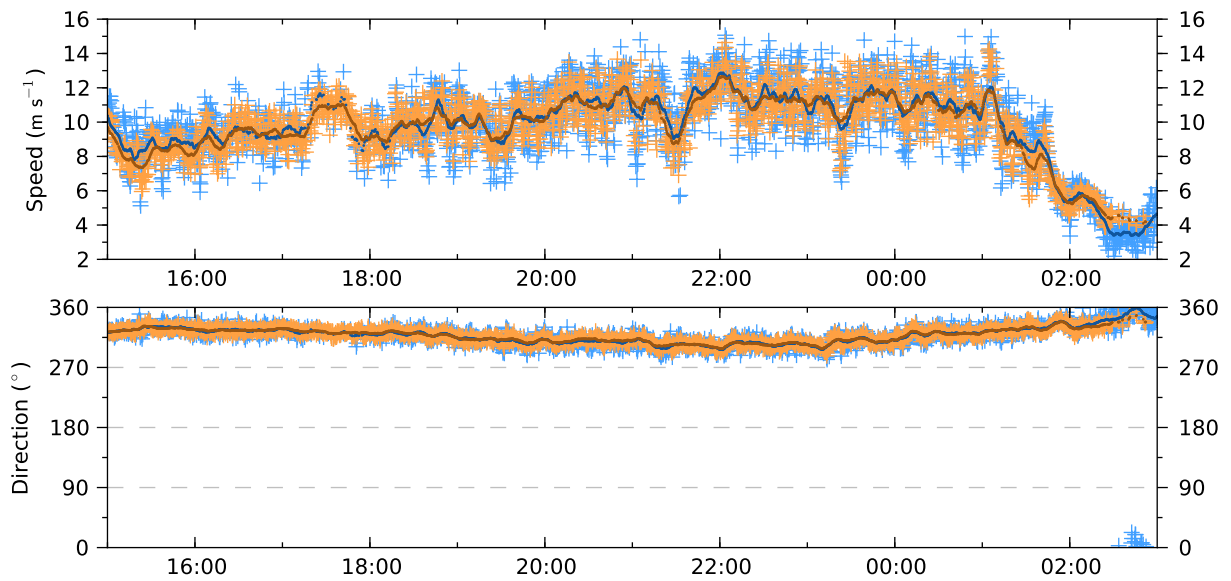


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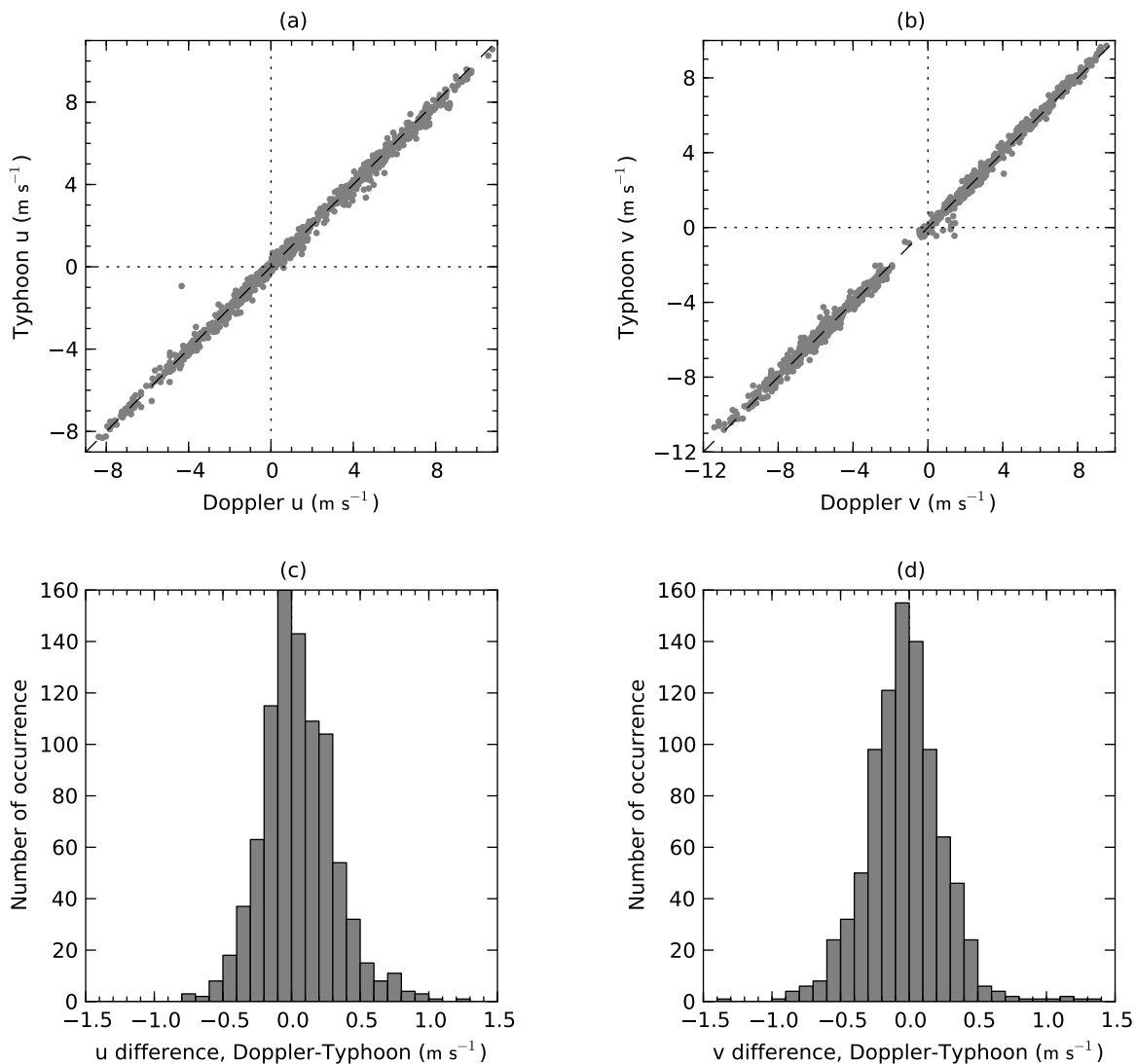


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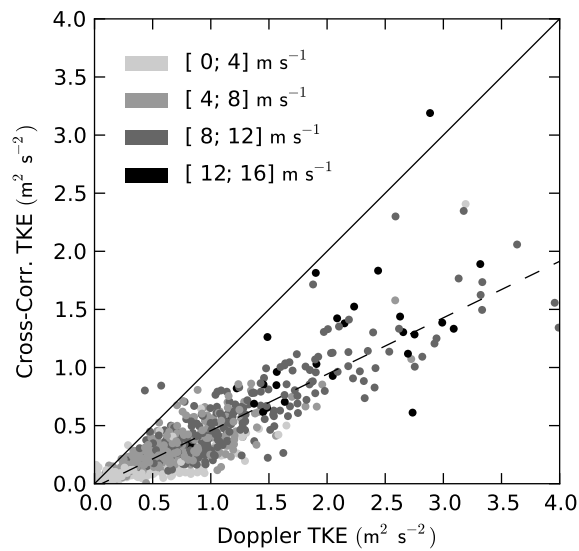




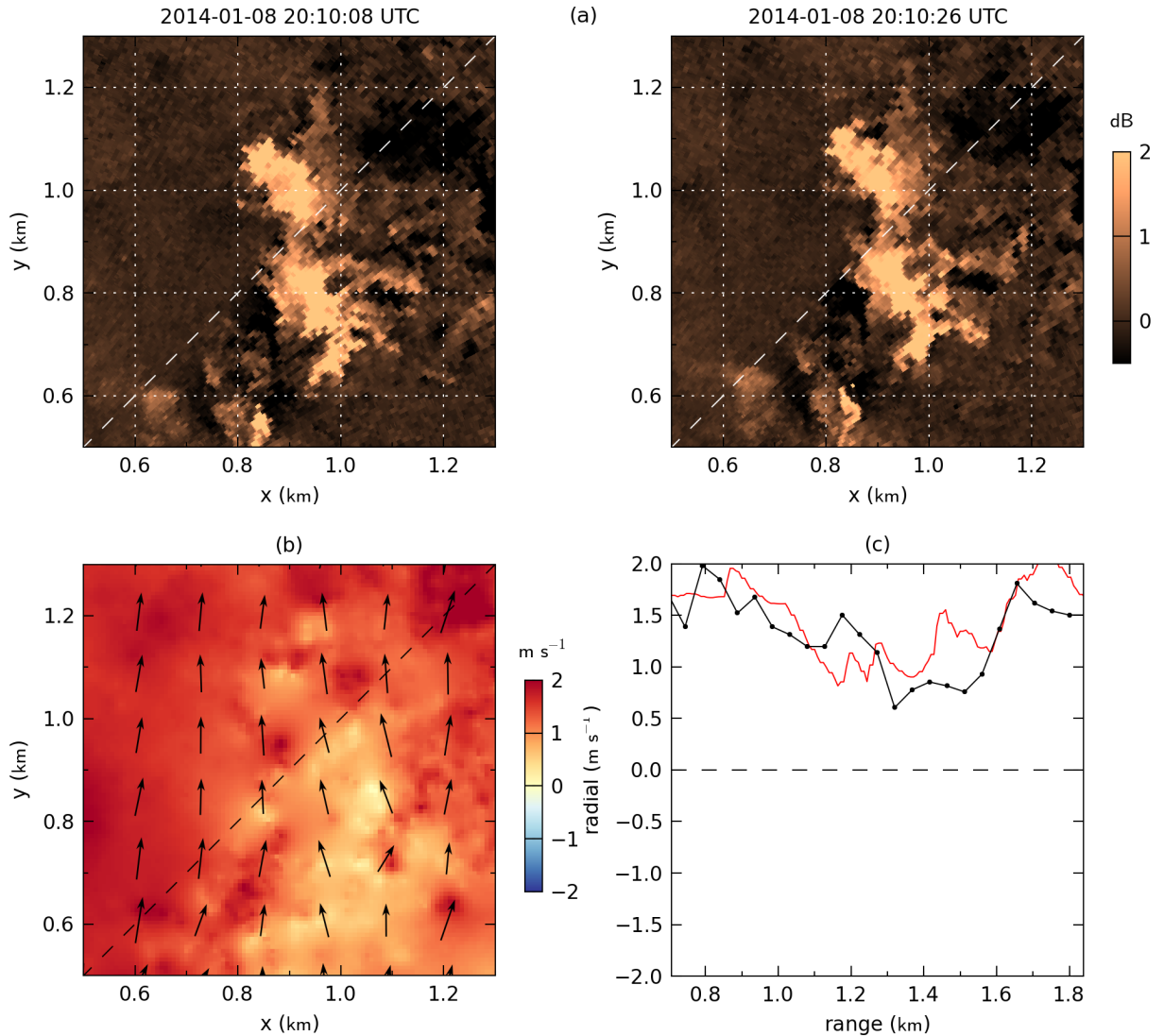
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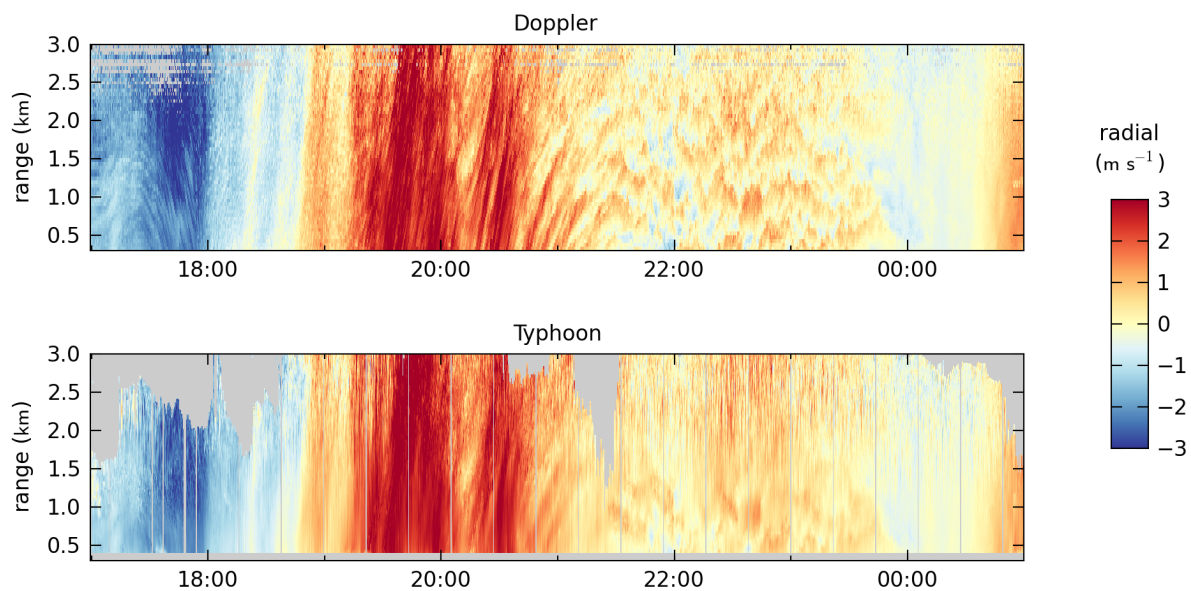
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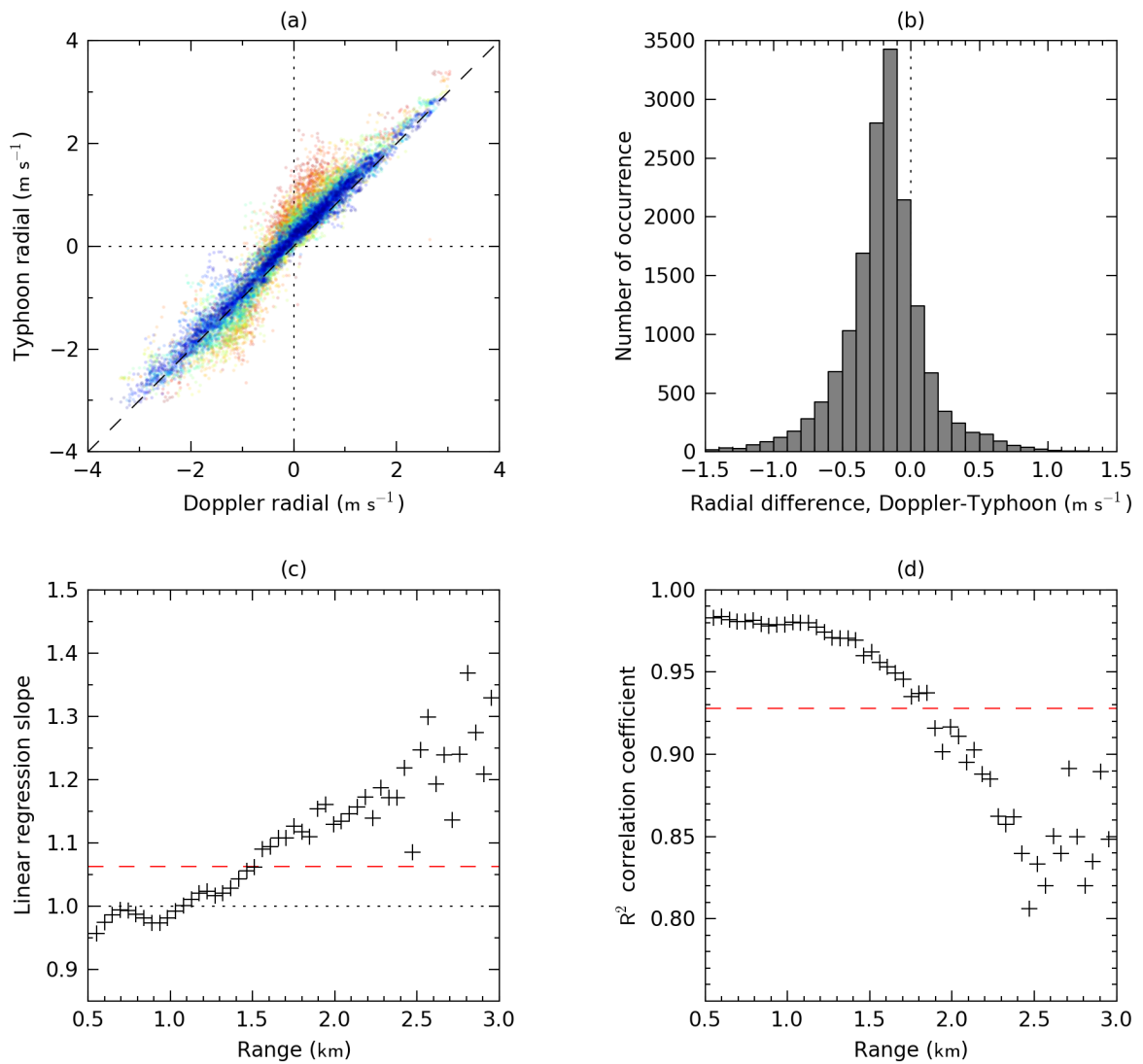
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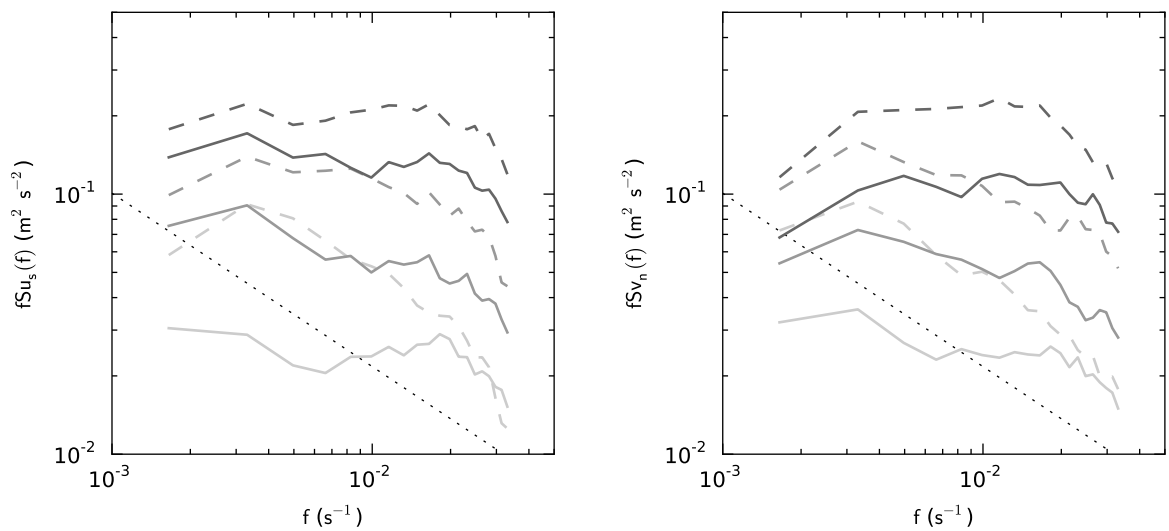
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 854 a close-up centered on the DL line-of-sight at  $45^\circ$  azimuth (dashed white line). The copper shading indicates  
 855 the intensity, in dB, of aerosol backscatter. A large aerosol feature is being advected north. Panel (b) shows the  
 856 velocity field (black arrows) estimated by *Typhoon* from these two scans; the vector field was decimated by a  
 857 factor of 15 along both dimensions for the sake of visualization. The color shading in the background indicates  
 858 the corresponding radial velocity. Panel (c) compares the radial velocities measured by the Doppler (black line)  
 859 and extracted from the 2-component field estimated by *Typhoon* (red line), along the DL line-of-sight.



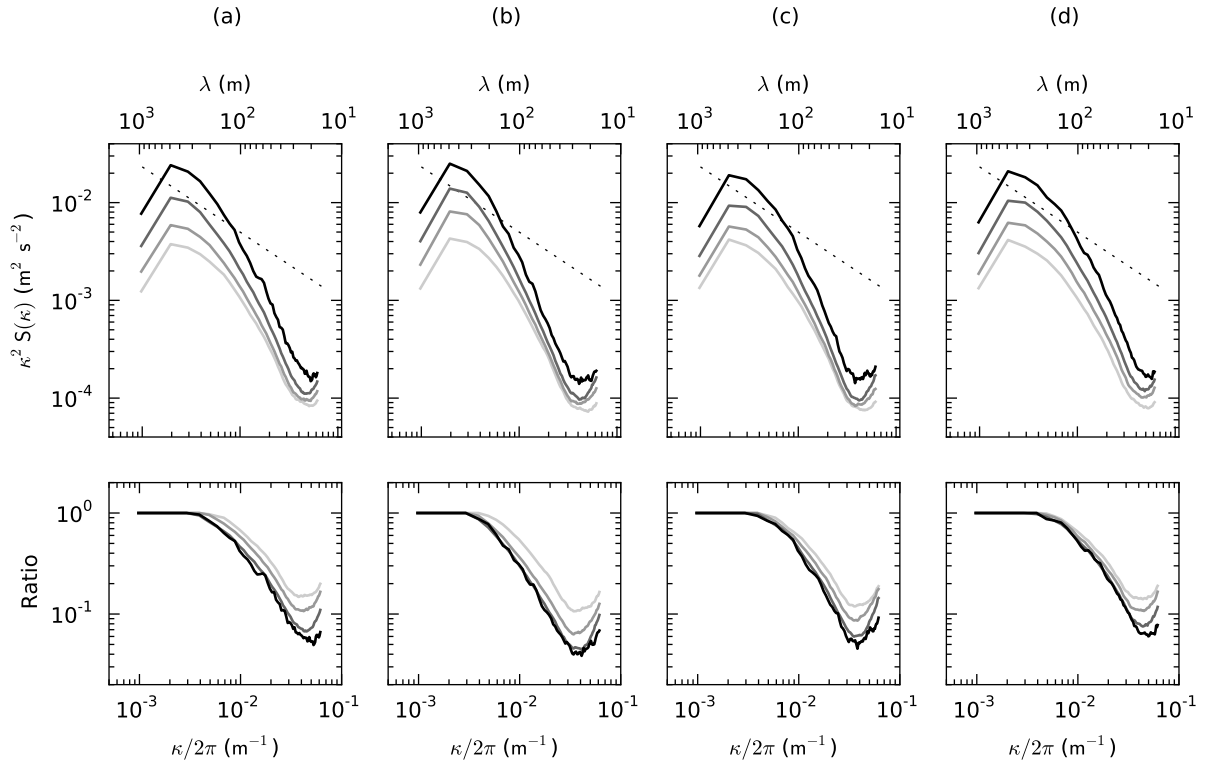
860 FIG. 12. Comparison of *radial wind component* at  $45^\circ$  azimuth and  $2^\circ$  elevation measured by the DL (top)  
 861 and estimated by proposed method (bottom), as a function of time (horizontal axis) and range (vertical axis), for  
 862 a 8-hour period starting 8 January 2014 at 17:00 UTC. Gray shading indicates missing or discarded data.



863 FIG. 13. Panel (a), scatter plot of 10-min averaged radial wind component measured by the DL (horizontal  
 864 axis) versus estimated by the proposed method (vertical axis). Color indicates the range, from blue (0.5 km) to  
 865 red (3 km). Panel (b), histogram of differences. Panel (c), slope of linear regression as a function of range. Panel  
 866 (d),  $R^2$  coefficient as a function of range. Dashed red lines indicate overall slope and  $R^2$  values.



867 FIG. 14. Temporal spectra for stream-wise component  $u_s$  (left) and cross-stream component  $v_n$  (right) obtained  
 868 by *Typhoon* (solid lines) and the DL (dashed lines). The shadings from light to dark gray correspond to wind  
 869 speed ranges of [0;4], [4;8], and [8;12]  $\text{m s}^{-1}$ . The dotted line represents the  $-2/3$  slope of the inertial subrange  
 870 predicted by theory.



871 FIG. 15. Slices of 2D power spectral density (top) and corresponding transfer functions (bottom), for stream-  
 872 wise component  $u$  in the streamwise (a) and cross-stream (b) directions, and cross-wise component  $v$  in the  
 873 streamwise (c) and cross-stream (d) directions. The shadings from light gray to black correspond to wind speed  
 874 ranges of  $[0;4]$ ,  $[4;8]$ ,  $[8;12]$  and  $[12;16]$   $\text{m s}^{-1}$ . The dotted line represents the  $-2/3$  slope of the inertial subrange  
 875 predicted by theory.